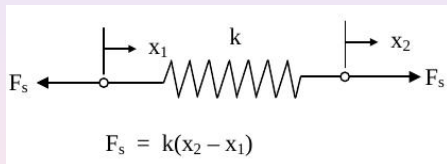


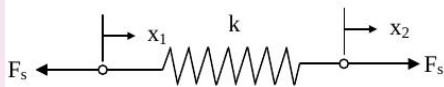
AE31002 Structural Dynamics

Anup Ghosh

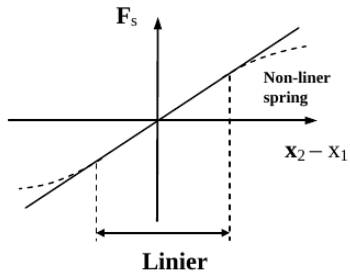
Discrete Systems and Spring



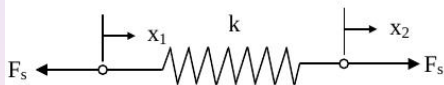
Discrete Systems and Spring



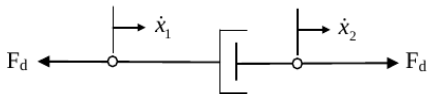
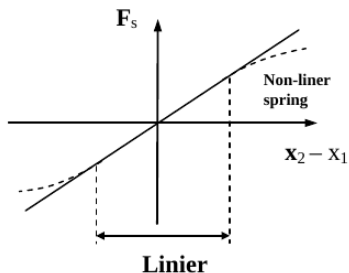
$$F_s = k(x_2 - x_1)$$



Discrete Systems and Spring

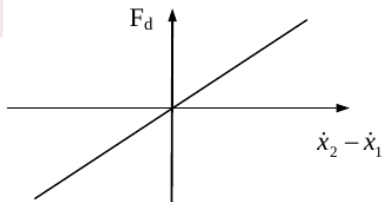
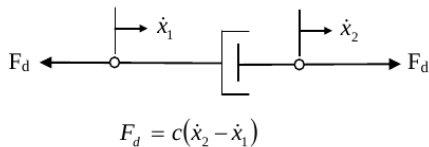
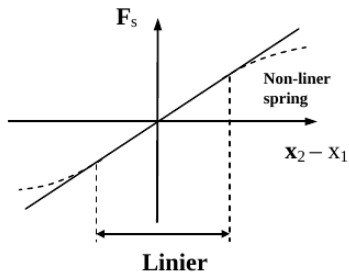
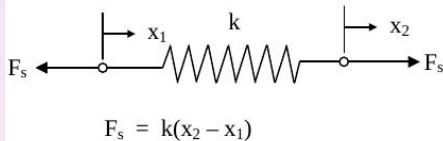


$$F_s = k(x_2 - x_1)$$



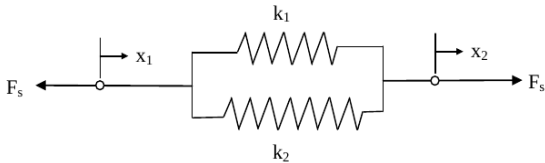
$$F_d = c(\dot{x}_2 - \dot{x}_1)$$

Discrete Systems and Spring

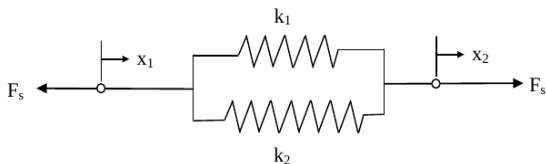


Parallel Springs

Parallel Springs

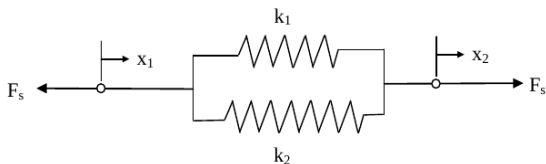


Parallel Springs



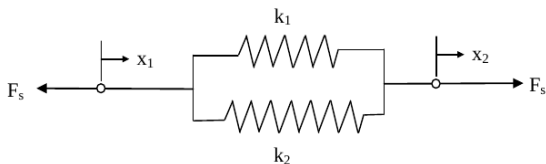
$$F_{s1} = k_1(x_2 - x_1) \text{ and}$$

Parallel Springs



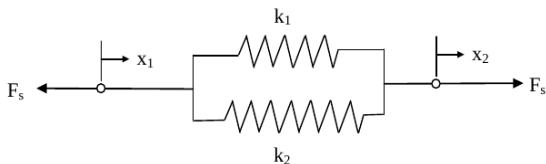
$$F_{s1} = k_1(x_2 - x_1) \text{ and } F_{s2} = k_2(x_2 - x_1)$$

Parallel Springs



$$F_{s1} = k_1(x_2 - x_1) \text{ and } F_{s2} = k_2(x_2 - x_1) \Rightarrow F_s = k_{eq}(x_2 - x_1)$$

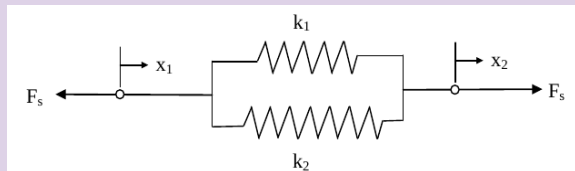
Parallel Springs



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Where $k_{eq} = k_1 + k_2$;

Parallel Springs



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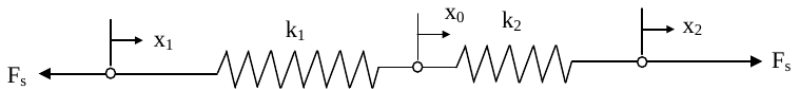
Where $k_{eq} = k_1 + k_2$;

Similarly for n number of parallel springs

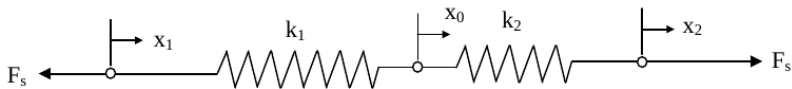
$$k_{eq} = \sum_{i=1}^n k_i$$

Springs in Series

Springs in Series

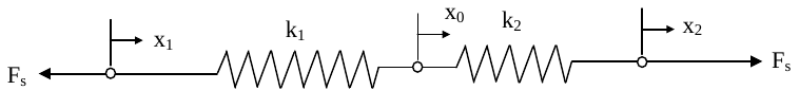


Springs in Series



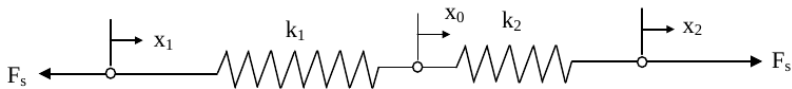
$$F_s = k_1(x_0 - x_1) \text{ and}$$

Springs in Series



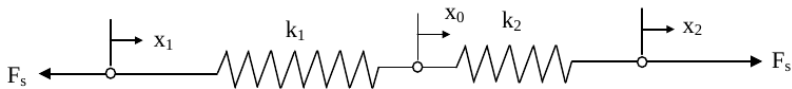
$$F_s = k_1(x_0 - x_1) \text{ and } F_s = k_2(x_2 - x_0)$$

Springs in Series



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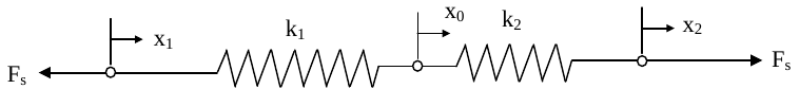
Springs in Series



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Springs in Series



$$F_s = k_1(x_0 - x_1) \text{ and } F_s = k_2(x_2 - x_0) \Rightarrow F_s = k_{eq}(x_2 - x_1)$$

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Similarly for n number of springs in series

$$k_{eq} = \left(\sum_{i=1}^n \frac{1}{k_i} \right)^{-1}$$

D'Alemberts's Principle

D'Alemberts's Principle

In the case of **static elastic deformation**, the internal **elastic forces**, try to restore the system to the position of equilibrium.

D'Alemberts's Principle

In the case of **pendulum**, restoring force is force of **gravity** (Rigid body motion).

D'Alemberts's Principle

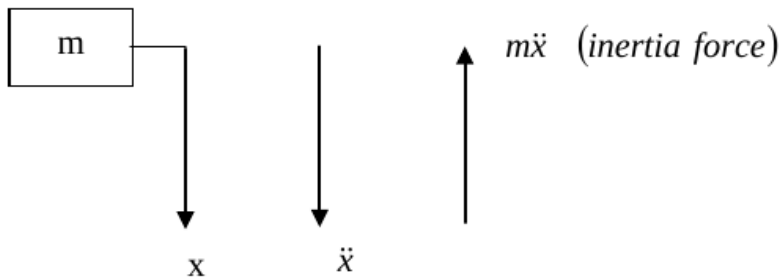
In the case of **vibration**, D'Alembert reasoned that the **sum of the forces** acting on a particle result in acceleration \ddot{x} . The inertial force can be computed by multiplying the mass of the body, $F = m\ddot{x}$.

D'Alembert's Principle

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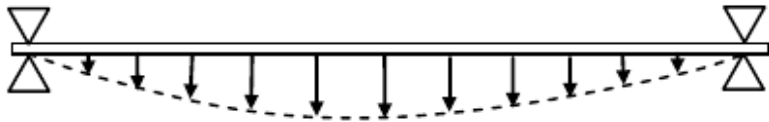
If the **force** so computed is applied to the body **at its mass center** in the direction **opposite to its acceleration**, the dynamic problem is reduced to one of statics. This is the D'Alembert principle.

D'Alemberts's Principle

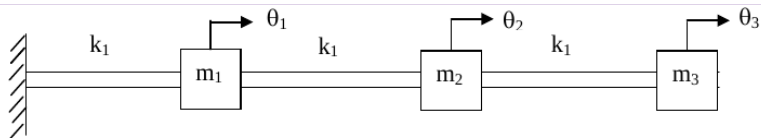
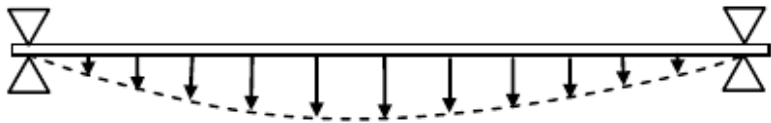


The number co-ordinates

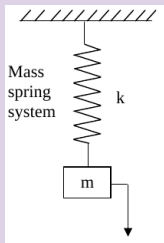
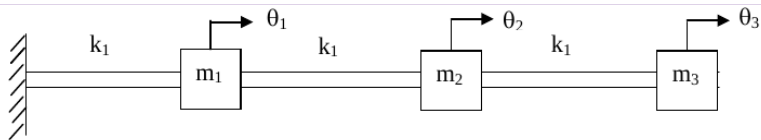
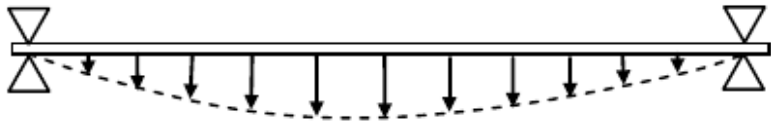
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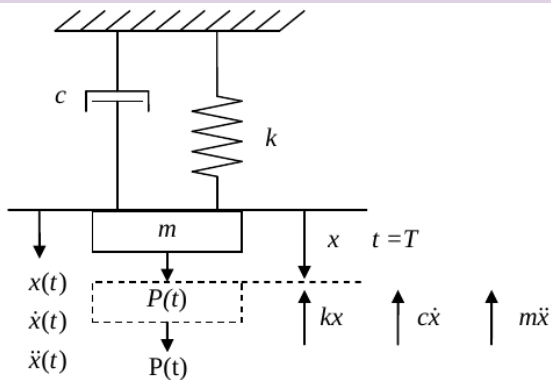


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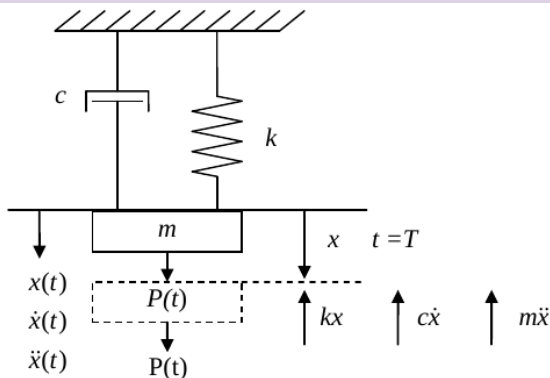


A SDOF System

A SDOF System



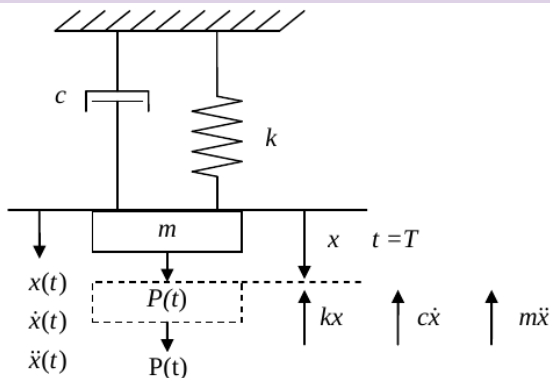
A SDOF System



Equilibrium equation

$m\ddot{x} + c\dot{x} + kx = P(t)$, — Dynamic Equilibrium Equation.

A SDOF System



Equilibrium equation

$m\ddot{x} + c\dot{x} + kx = P(t)$, — Dynamic Equilibrium Equation.

If $p(t) = 0$, it is free vibration.